# YEAR 12 | A LEVEL FURTHER MATHS

The curriculum and assessment of students at this stage of education has been carefully designed to promote deep learning of mathematics and develop students into mathematicians:

Scheme of work follows the 2017 specification from Edexcel, which builds on prior knowledge from GCSE. There are opportunities throughout to apply techniques and methods to real life modelling.

### HALF TERM 1

#### All students will know:

#### CORE

#### 1) Complex numbers:

- » Understand and use definitions of imaginary and complex numbers.
- » Add, subtract, multiply with complex numbers.
- » Understand complex conjugates and use in division of complex numbers.
- » Solve quadratic, cubic and quartic equations with complex roots.

#### 2) Argand diagrams:

- » Show complex numbers on an Argand diagram.
- Find the modulus and argument of a complex number, and write in modulus-argument form.
- » Represent loci and regions on an Argand diagram.

#### DISCRETE

#### 1) Algorithms:

- » Understand and use an algorithm given in words, or using a flow chart.
- » Carry out a bubble sort and a quick sort.
- » Carry out the three bin-packing algorithms and understand their strengths and weaknesses.
- » Determine the order of an algorithm.

#### 2) Graphs and networks:

- » Know how mathematical models use graphs and networks, and be familiar with basic graph theory terminology.
- » Know how matrices can be used to represent graphs and networks.

#### 3) Algorithms on graphs:

- » Use Kruskal's algorithm and Prim's algorithm to find a minimum spanning tree.
- » Apply Prim's algorithm to a distance matrix.
- » Use Dijkstra's algorithm to find the shortest path between two vertices in a network.
- » Use Floyd's algorithm.

## All students will be assessed:

Class assessments on all the topics covered during this half term.

Past paper questions on topics covered.

## Reading skills needed for this unit:

Pearson eBook.

#### Key vocabulary:

Complex, imaginary, conjugate, real, Argand diagram, argument, algorithm, modulus, loci, region.

### CURRICULUM AND ASSESSMENT PLAN YEAR 12 | FURTHER MATHS

### **ENRICHMENT OPPORTUNITIES**

UKMT challenge, university lecture visits.

### HALF TERM 2

#### All students will know:

#### CORE

#### 1) Series:

- » Use the standard results for the sum of natural numbers, square numbers and cube numbers.
- » Simplify a series that is of a linear, quadratic or cubic form.

#### 2) Roots of polynomials

- » Derive and use the relationship between coefficients and roots of quadratic, cubic and quartic equations.
- » Evaluate expressions relating to the roots of a polynomial.
- » Find the equation of a polynomial whose roots are a linear transformation of another polynomial.

#### DISCRETE

#### 1) Route inspection:

- » Use orders of nodes to determine whether a graph is Eulerian, semi-Eulerian or neither.
- » Use the Chinese postman algorithm to find the shortest route in a network.
- » Use route inspection algorithms in networks with more than four odd nodes.

#### 2) Linear programming:

- » Model a problem using linear programming.
- » Illustrate a two-variable linear programming problem graphically.
- » Locate the optimal point in a feasibility region using the objective line (ruler) method, and the vertex testing method.
- » Determine solutions that need integer values.

## All students will be assessed:

Class assessments on all the topics covered during this half term.

Past paper questions on topics covered.

## Reading skills needed for this unit:

Pearson eBook.

#### Key vocabulary:

Series, sigma, summation, convergence, divergence, roots, coefficient, integer, rational.

### HALF TERM 3

#### All students will know:

#### CORE

#### 1) Volume of revolutions:

- » Find the volume of revolution when a curve is rotated about the x-axis or the y-axis.
- » Find more complex volumes through addition and subtraction of volume of revolutions.
- » Model real-life situations using volumes of revolutions.

#### DISCRETE

#### 1) Critical path analysis:

- » Model a project by an activity network using a precedence table.
- » Use dummy activities.
- » Identify and calculate early and late event times in activity networks, and critical activities.
- » Calculate total float of an activity.
- » Calculate and use Gantt (cascade) charts

#### MECHANICS

#### 1) Momentum and impulse:

- » Calculate the momentum of a particle and the impulse of a force.
- » Solve problems involving collisions using conservation of momentum.

## All students will be assessed:

Class assessments on all the topics covered during this half term.

Past paper questions on topics covered.

## Reading skills needed for this unit:

Pearson eBook.

#### Key vocabulary:

Calculus, volume, revolution, solid, radian, integration, integral, definite and indefinite.

### CURRICULUM AND ASSESSMENT PLAN YEAR 12 | FURTHER MATHS

### **HALF TERM 4**

#### All students will know:

#### CORE

#### 1) Matrices:

- » Understand the concept of a matrix, including zero and identity matrices.
- » Add, subtract and multiply matrices.
- » Find the determinant of a matrix, and the inverse of a matrix.
- » Use matrices to form simultaneous equations, and interpret them geometrically.

#### 2) Linear transformations:

- » Understand the properties of linear transformations and represent them using matrices, including in 3D.
- » Reflect, rotate and stretch using matrices.
- » Find invariant points and lines.
- » Carry out successive transformations, and use inverse matrices to reverse a transformation.

#### MECHANICS

#### 1) Work, energy and power:

- » Calculate the work done by a force.
- » Calculate the kinetic energy and potential energy of a particle.
- » Use conservation of energy and the work-energy principle.
- » Calculate the power developed by an engine.

## All students will be assessed:

Class assessments on all the topics covered during this half term.

Past paper questions on topics covered

## Reading skills needed for this unit:

Pearson eBook.

#### Key vocabulary:

Matrix, vector, determinant, minor, cofactors, transpose, inverse, identity, zero matrix, lead diagonal, plane, coplanar, singular / non-singular, consistent, translation, reflection, rotation, stretch, invariant, momentum, impulse, conservation, work done, power, kinetic energy, potential energy.

### HALF TERM 5

#### All students will know:

#### CORE

- 1) Proof by induction:
- » Understand the principle of proof by induction and use to prove the sum of a series.
- » Prove results about divisibility using induction.
- » Prove results about matrices using matrices.

#### CORE

#### 1) Vectors:

- » Understand and use vector and Cartesian forms of theequation of a straight line in 3D and of a plane.
- » Calculate the scalar product for two 3D vectors, and use it bfind the angle between lines and planes.
- » Determine whether two lines meet and the point of intersection.
- » Calculate the perpendicular distance between two lines, a point to a line, or a point to a plane.

#### MECHANICS

#### 1) Elastic collisions in 1D:

- » Solve problems involving collisions of two particles using conservation of momentum and Newton's law of restitution.
- » Find the change in energy due to an impact or application of an impulse.
- Solve problems involving successive impacts.

## All students will be assessed:

Class assessments on all the topics covered during this half term.

Past paper questions on topics covered.

External examinations will take place in May/June for those students not wishing to continue to A Level.

Reading skills needed for this unit:

Pearson eBook.

#### Key vocabulary:

Proof by induction, argument, statement, example, contradiction, elasticity, plastic, tension, work done, static, dynamic, potential energy, kinetic energy, momentum, vector, cartesian, plane,coplanar, intersection, collision, elastic, plastic, impulse, oblique, conservation.

### HALF TERM 6

#### All students will know:

#### CORE

#### 1) Further Complex Numbers

» Exponential forms of complex numbers

Multiplying and dividing complex numbers

De Moivre's Theorem

Trigonometric identities

#### MECHANICS

#### 1) Momentum and Impulse:

» Momentum as a vector

#### All students will be assessed:

External examinations will take place in May for those students not wishing to continue to A Level.

» Class assessments onall the topics covered during this half term.

Past paper questions on topics covered

» For those continuing to A Level, the summer mock exam will assess the full content of the AS course using AS-level past examination papers.

#### Reading skills neededfor this unit:

Pearson eBook.

## HOW STUDENTS CAN BE SUPPORTED AT HOME

Pearson Active Learn eBooks, videos of class assessment model answers, independent study guide with suggested websites.